

2)

AP Test Question 2008 Part A - With Calculator

|                 |     |     |     |     |     |    |   |
|-----------------|-----|-----|-----|-----|-----|----|---|
| t (hours)       | 0   | 1   | 3   | 4   | 7   | 8  | 9 |
| $L(t)$ (people) | 120 | 156 | 176 | 126 | 150 | 80 | 0 |

- 2) Concert tickets went on sale at noon ( $t = 0$ ) and were sold out within 9 hours. The number of people waiting in line to purchase tickets at time  $t$  is modeled by a twice-differentiable function  $L$  for  $0 \leq t \leq 9$ . Values of  $L(t)$  at various times  $t$  are shown in the table above.
- a) Use the data in the table to estimate the rate at which the number of people waiting in line was changing at 5:30 P.M. ( $t = 5.5$ ). Show the computations that lead to your answer. Indicate units of measure. **8 people/hour**

|                 |     |     |     |     |     |    |   |
|-----------------|-----|-----|-----|-----|-----|----|---|
| t (hours)       | 0   | 1   | 3   | 4   | 7   | 8  | 9 |
| $L(t)$ (people) | 120 | 156 | 176 | 126 | 150 | 80 | 0 |

- b) Use a trapezoidal sum with three subintervals to estimate the average number of people waiting in line during the first 4 hours that tickets were on sale. **155 people**

|                 |     |     |     |     |     |    |   |
|-----------------|-----|-----|-----|-----|-----|----|---|
| t (hours)       | 0   | 1   | 3   | 4   | 7   | 8  | 9 |
| $L(t)$ (people) | 120 | 156 | 176 | 126 | 150 | 80 | 0 |

- c) For  $0 \leq t \leq 9$ , what is the fewest number of times at which  $L'(t)$  must equal 0? Give a reason for your answer. **3 times**

|                 |     |     |     |     |     |    |   |
|-----------------|-----|-----|-----|-----|-----|----|---|
| t (hours)       | 0   | 1   | 3   | 4   | 7   | 8  | 9 |
| $L(t)$ (people) | 120 | 156 | 176 | 126 | 150 | 80 | 0 |

- d) The rate at which tickets were sold for  $0 \leq t \leq 9$  is modeled by  $r(t) = 550te^{-\frac{t}{2}}$  tickets per hour. Based on the model, how many tickets were sold by 3 P.M. ( $t = 3$ ), to the nearest whole number? **973 tickets**